

THE CHOICE OF OPTIMAL DECISIONS ÎN UNCERTITUDE SITUATIONS

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Abstract: *The Electre method is a classical algorithm for the decidence of a suitable choice in the process of launching on market of some products. In this paper I shall give a variation of the last part of the algorithm in the direction of simplifying the finally computations.*

In many practical situations, it exists many informations refered to the actions which can be developed, but for each action choice it exists many possibilities.

The Electre method gives us a way which will make out between different possibilities.

Let therefore n choices V_1, V_2, \dots, V_n for a decident. We have also m criterions C_1, C_2, \dots, C_m who have, each of them, a weighty coefficient (by rule subjective assigned) k_1, k_2, \dots, k_m .

For each pair (V_i, C_j) we have a numerical value (if it is a qualitative estimation we shall convert in hierarchy numbers).

The algorithm will determine the best choice of action.

Step I

We settle, for the beginning the method nature: maximisation or minimisation. We shall add two lines under the table, on which will compute the maximum and the minimum of all numbers on columns.

Step II

We shall determine the utilities U_{ij} corresponding to all pairs (V_i, C_j) :

- ◆ for the maximisation problem:
$$U_{ij} = \frac{v_{ij} - \min_{k=1, \dots, n} v_{kj}}{\max_{k=1, \dots, n} v_{kj} - \min_{k=1, \dots, n} v_{kj}};$$
- ◆ for the minimisation problem:
$$U_{ij} = \frac{\max_{k=1, \dots, n} v_{kj} - v_{ij}}{\max_{k=1, \dots, n} v_{kj} - \min_{k=1, \dots, n} v_{kj}}.$$

and after we shall draw the table with these results.

Step III

We shall compute the correspondence indicators: $c(V_i, V_j) = \frac{\sum_{p=1, \dots, m}^{U_{ip} \geq U_{jp}} k_p}{\sum_{r=1}^m k_r}$ and after the disunity

indicators: $d(V_i, V_j) = \max_{p=1, \dots, m} (U_{jp} - U_{ip}, 0)$.

Step IV

We shall draw a new table for each pair (V_i, V_j) where on each cell we shall write on the left the correspondence indicator and on the right the disunity indicator.

Step V

We shall establish two values p and q (with a significance of complementary probabilities) such that $p, q \in (0, 1)$ and $p + q = 1$ which will extent the admissible limits for correspondence, respectively disunity. We shall say that V_i is better than V_j if

$$\begin{cases} c(V_i, V_j) \geq p \\ d(V_i, V_j) \leq q \end{cases}$$

Let now the matrix $G=(g_{ij}) \in M_n(\mathbf{R})$ such that: $g_{ij}=1$ if V_i is better than V_j and 0 in the other situations. If it exists a row i with all elements equal with 1 it follows that V_i is better than all others therefore it will be preferred. If it does not exist such a V_i we shall diminish the value of p (and of course increase q) till we shall obtain the better choice.

In what follows I shall present another way to choose p and q .

The system: $\begin{cases} c(V_i, V_j) \geq p \\ d(V_i, V_j) \leq q \end{cases}$ can be written as: $\begin{cases} c(V_i, V_j) \geq p \\ d(V_i, V_j) \leq 1-p \end{cases}$ therefore:

$$p \leq \min(c(V_i, V_j), 1-d(V_i, V_j))$$

We shall compute $\min_{j=1,n} c(V_i, V_j)$ and $\min_{j=1,n} (1-d(V_i, V_j))$ from where:

$$p \leq \min(\min_{j=1,n} c(V_i, V_j), 1 - \max_{j=1,n} d(V_i, V_j))$$

In the last table, we shall add therefore three columns, on which we compute $\min_{j=1,n} c(V_i, V_j)$, $1 - \max_{j=1,n} d(V_i, V_j)$ and the minimum of these two values. The better choice will be those who give the maximum value on this last column.

Example

Let the following problem (of maximisation):

Criterion Choice	C_1 ($k_1=0,4$)	C_2 ($k_2=0,4$)	C_3 ($k_3=0,2$)
V_1	1000	0	50
V_2	800	1	56
V_3	600	2	60
V_4	700	1	54
V_5	500	2	58

Criterion Choice	C_1	C_2	C_3
V_1	1000	0	50
V_2	800	1	56
V_3	600	2	60
V_4	700	1	54
V_5	500	2	58
min	500	0	50
max	1000	2	60
max-min	500	2	10

The utilities table is:

Criterion Choice	C_1 ($k_1=0,4$)	C_2 ($k_2=0,4$)	C_3 ($k_3=0,2$)
V_1	1	0	0
V_2	0,6	0,5	0,6
V_3	0,2	1	1
V_4	0,4	0,5	0,4
V_5	0	1	0,8

And the table of correspondence indicators and the disunity indicators:

	V_1		V_2		V_3		V_4		V_5	
V_1	1	0	0,4	0,6	0,4	1	0,4	0,5	0,4	1
V_2	0,6	0,4	1	0	0,4	0,5	1	0	0,4	0,5

V_3	0,6	0,8	0,6	0,4	1	0	0,6	0,2	1	0
V_4	0,6	0,6	0,4	0,2	0,4	0,6	1	0	0,4	0,5
V_5	0,6	1	0,6	0,6	0,4	0,2	0,6	0,4	1	0

If we try for p from 1 back to 0 we shall obtain that, for the first time, we shall have for p=0,4 and q=0,6:

$$G = \begin{pmatrix} 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 1 \end{pmatrix}$$

therefore each of V_2 and V_4 is better than the others.

I shall suggest at this last step the following:

	V_1		V_2		V_3		V_4		V_5		$\min_{j=1,n} c(V_i, V_j)$	$\max_{j=1,n} d(V_i, V_j)$	min
V_1	1	0	0,4	0,6	0,4	1	0,4	0,5	0,4	1	0,4	1	0
V_2	0,6	0,4	1	0	0,4	0,5	1	0	0,4	0,5	0,4	0,5	0,4
V_3	0,6	0,8	0,6	0,4	1	0	0,6	0,2	1	0	0,6	0,8	0,2
V_4	0,6	0,6	0,4	0,2	0,4	0,6	1	0	0,4	0,5	0,4	0,6	0,4
V_5	0,6	1	0,6	0,6	0,4	0,2	0,6	0,4	1	0	0,4	1	0

therefore each of V_2 and V_4 is better than the others, but without consecutive tests.